

# mixing



# flavor mixing angles fermion masses









### ass mat r ces



**U,C - (**,S

### H. Fritzsch S. Weinberg 78 <u>G</u>)











### lefthanded and righthanded neutrinos

Electroweak theory:

### SU(2)<sub>L</sub>x SU(2)<sub>R</sub>x U(1) ((1)) ((1)) (1

Weak gauge group: SU(2), × SU(2), × U(1)

2 scalars:

 $\left(\frac{1}{2},\frac{1}{2}\right)$ 

 $U = \begin{pmatrix} U_{11} & U_{12} \\ U_{21} & U_{22} \end{pmatrix} \quad V = \begin{pmatrix} V_{11} & V_{12} \\ V_{21} & V_{22} \end{pmatrix}$ 

### Interaction

 $g_1(u_o, d_o)_L U \begin{pmatrix} u_o \\ d_o \end{pmatrix}_R + g_2(u_o, d_o)_L U \begin{pmatrix} u_o \\ s \end{pmatrix}_R$  $+g_{3}(c_{o},s_{o})_{L} \left( \begin{pmatrix} u_{o} \\ d_{o} \end{pmatrix}_{R} + g_{4}(c_{o},s_{o})_{L} \left( \begin{pmatrix} c_{o} \\ s_{o} \end{pmatrix}_{R} \end{pmatrix} \right)_{L} \left( \begin{pmatrix} u_{o} \\ s_{o} \end{pmatrix}_{R} + g_{4}(c_{o},s_{o})_{L} \left( \begin{pmatrix} c_{o} \\ s_{o} \end{pmatrix}_{R} \right)_{L} \right)_{L} \left( \begin{pmatrix} u_{o} \\ s_{o} \end{pmatrix}_{R} + g_{4}(c_{o},s_{o})_{L} \right)_{L} \left( \begin{pmatrix} u_{o} \\ s_{o} \end{pmatrix}_{R} + g_{4}(c_{o},s_{o})_{L} \right)_{L} \left( \begin{pmatrix} u_{o} \\ s_{o} \end{pmatrix}_{R} + g_{4}(c_{o},s_{o})_{L} \right)_{L} \left( \begin{pmatrix} u_{o} \\ s_{o} \end{pmatrix}_{R} + g_{4}(c_{o},s_{o})_{L} \right)_{L} \left( \begin{pmatrix} u_{o} \\ s_{o} \end{pmatrix}_{R} + g_{4}(c_{o},s_{o})_{L} \right)_{L} \left( \begin{pmatrix} u_{o} \\ s_{o} \end{pmatrix}_{R} + g_{4}(c_{o},s_{o})_{L} \right)_{L} \left( \begin{pmatrix} u_{o} \\ s_{o} \end{pmatrix}_{R} + g_{4}(c_{o},s_{o})_{L} \right)_{L} \left( \begin{pmatrix} u_{o} \\ s_{o} \end{pmatrix}_{R} + g_{4}(c_{o},s_{o})_{L} \right)_{L} \left( \begin{pmatrix} u_{o} \\ s_{o} \end{pmatrix}_{R} + g_{4}(c_{o},s_{o})_{L} \right)_{L} \left( \begin{pmatrix} u_{o} \\ s_{o} \end{pmatrix}_{R} + g_{4}(c_{o},s_{o})_{L} \right)_{L} \left( \begin{pmatrix} u_{o} \\ s_{o} \end{pmatrix}_{R} + g_{4}(c_{o},s_{o})_{L} \right)_{L} \left( \begin{pmatrix} u_{o} \\ s_{o} \end{pmatrix}_{R} + g_{4}(c_{o},s_{o})_{L} \right)_{L} \left( \begin{pmatrix} u_{o} \\ s_{o} \end{pmatrix}_{R} + g_{4}(c_{o},s_{o})_{L} \right)_{L} \left( \begin{pmatrix} u_{o} \\ s_{o} \end{pmatrix}_{R} + g_{4}(c_{o},s_{o})_{L} \right)_{L} \left( \begin{pmatrix} u_{o} \\ s_{o} \end{pmatrix}_{R} + g_{4}(c_{o},s_{o})_{L} \right)_{L} \left( \begin{pmatrix} u_{o} \\ s_{o} \end{pmatrix}_{R} + g_{4}(c_{o},s_{o})_{L} \right)_{L} \left( \begin{pmatrix} u_{o} \\ s_{o} \end{pmatrix}_{R} + g_{4}(c_{o},s_{o})_{L} \right)_{L} \left( \begin{pmatrix} u_{o} \\ s_{o} \end{pmatrix}_{R} + g_{4}(c_{o},s_{o})_{L} \right)_{L} \left( \begin{pmatrix} u_{o} \\ s_{o} \end{pmatrix}_{R} + g_{4}(c_{o},s_{o})_{L} \right)_{L} \left( \begin{pmatrix} u_{o} \\ s_{o} \end{pmatrix}_{R} + g_{4}(c_{o},s_{o})_{L} \right)_{L} \left( \begin{pmatrix} u_{o} \\ s_{o} \end{pmatrix}_{R} + g_{4}(c_{o},s_{o})_{L} \right)_{L} \left( \begin{pmatrix} u_{o} \\ s_{o} \end{pmatrix}_{R} + g_{4}(c_{o},s_{o})_{L} \right)_{L} \left( \begin{pmatrix} u_{o} \\ s_{o} \end{pmatrix}_{R} + g_{4}(c_{o},s_{o})_{L} \right)_{L} \left( \begin{pmatrix} u_{o} \\ s_{o} \end{pmatrix}_{R} + g_{4}(c_{o},s_{o})_{L} \right)_{L} \left( \begin{pmatrix} u_{o} \\ s_{o} \end{pmatrix}_{L} \right)_{L}$  $+h.c. + U \rightarrow V, g, \rightarrow g', etc.$ +  $g_5(u_o, d_o)_L T_2 U^+ T_2 (d_o)_R + \cdots$  $+ U \rightarrow V^{+}, g_{5} \rightarrow g_{5}^{\prime}.$ 

U(1) x U(1) symmetry  $\begin{pmatrix} u_{\circ} \\ d_{\circ} \end{pmatrix}_{L} \rightarrow e^{i \alpha} \begin{pmatrix} u_{\circ} \\ d_{\circ} \end{pmatrix}_{L} \begin{pmatrix} u_{\circ} \\ d_{\circ} \end{pmatrix}_{L} \rightarrow e^{-i \alpha} \begin{pmatrix} u_{\circ} \\ d_{\circ} \end{pmatrix}_{R} \rightarrow e^{-i \alpha} \begin{pmatrix} u_{\circ} \\ d_{\circ} \end{pmatrix}_{R}$  $\begin{pmatrix} c_{\circ} \\ s_{\circ} \end{pmatrix}_{L} \rightarrow e^{i\beta} \begin{pmatrix} c_{\circ} \\ s_{\circ} \end{pmatrix}_{L} \quad \begin{pmatrix} c_{\circ} \\ s_{\circ} \end{pmatrix}_{R} \rightarrow e^{-i\beta} \begin{pmatrix} c_{\circ} \\ s_{\circ} \end{pmatrix}_{R}$ V-> e'(x+B)V  $U \rightarrow e^{2\beta i U}$ 

 $g(c_{o}, s_{o})_{L} \begin{pmatrix} c_{o} \\ s_{o} \end{pmatrix}_{R} + h(c_{o}, s_{o})_{L} \bigvee \begin{pmatrix} u_{o} \\ u_{o} \end{pmatrix}_{R}$  $+h'(u_{o},ol_{O})_{C}V(s_{o})_{R}+h.c.$ 



Mixing angles <=> masses  $\begin{pmatrix} 0 & a \\ a^{\otimes} & b \end{pmatrix} = \begin{pmatrix} -m_u & 0 \\ 0 & m_c \end{pmatrix}$  $\tan 2\theta_u = \frac{2\sqrt{m_u m_c}}{m_c - m_u}$  $\theta_u \approx \sqrt{\frac{m_u}{m_c}}$ 

 $\frac{m_d}{m_s} \approx 0.21$ 

*m*<sub>u</sub>

### Cabibbo angle 13°

 $\theta_c \cong \left| \begin{array}{c} \frac{m_d}{m_s} - e^{i\phi} \\ \frac{m_u}{m_c} \end{array} \right| \frac{m_u}{m_c}$ 



m<sub>u</sub>

 $M_{c}$ 







### 6 leptons – 6 quarks

 $\begin{array}{ccc} u & c & t \\ d' & s' & b' \end{array}$  ${\cal V}_{\mu}$ ublets

1 1 S flavor mixing 1 S



### weak transitions and weak mixing

### **CKM-matrix**

 $\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$ 

### observed CKM – matrix





# CKM - matrix

# three angles - one phase

### **CKN matrix** standard parametrization $angles: \theta_{12}, \theta_{23}, \theta_{13}$

$$V = \begin{bmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{bmatrix} \bullet \begin{bmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{bmatrix} \bullet \begin{bmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

### New parametrization:

 $V = \begin{bmatrix} c_u & s_u & 0 \\ -s_u & c_u & 0 \\ 0 & 0 & 1 \end{bmatrix} \bullet \begin{bmatrix} e^{-i\phi} & 0 & 0 \\ 0 & c & s \\ 0 & -s & c \end{bmatrix} \bullet \begin{bmatrix} c_d & -s_d & 0 \\ s_d & c_d & 0 \\ 0 & 0 & 1 \end{bmatrix}$ H. Fritzsch - Z. Xing

## texture zeros: $\begin{pmatrix} 0 & A \\ A^* & C \\ 0 & B^* \end{pmatrix}$ 0 B D

\* B  $\boldsymbol{m}_d$  $rac{V_{ub}}{V}$ td m<sub>u</sub> V $m_{s}$ ts

 $\tan \theta_d = \sqrt{m_d} / \sqrt{m_s}$  $\tan \theta_{\mu} = \sqrt{m_{\mu}} / \sqrt{m_{c}}$ 



# $\theta_{\mu}$ $\theta_{d}$ have been measured separately.



 $\tan \theta_d = \sqrt{m_d} / \sqrt{m_s}$ 

# $\theta_d \approx 13.0 \pm 0.4^\circ$

# $\theta_d \approx 13.0 \pm 0.4^{\circ}$

# $Exp: 11.7^{\circ} \pm 2.6^{\circ}$

 $\tan \theta_u = \sqrt{m_u} / \sqrt{m_c}$ 

# $\theta_u \approx 5.0^o \pm 0.7^o$
# $\theta_{u} \approx 5.0^{\circ} \pm 0.7^{\circ}$

## $Exp: 5.4^{\circ} \pm 1.1^{\circ}$





#### alpha: 86 ... 95 degrees



# Unitarity triangle: $\tan \beta = \frac{\sin \theta_u \cos \theta_d}{\cos \theta_u \sin \theta_d}$

#### $\sin 2\beta \cong 0.663$

==>

#### $Exp: \sin 2\beta = 0.681 \pm 0.025$

 $\phi \approx \alpha = 90^{\circ}$ 

# Maximal CP-violation



# Standard Model

#### neutrinos => lefthanded

# no mass





#### Since 1998:

# Observation of neutrino oscillations in Kamioka (Japan)

## Neutrinos must have a mass

 $\mathcal{U}$ C  $d\cos\theta_c + s\sin\theta_c / \langle -d\sin\theta_c + s\cos\theta_c \rangle$ 

# $v_e = \cos\theta \cdot v_1 + \sin\theta \cdot v_2$ $v_\mu = -\sin\theta \cdot v_1 + \cos\theta \cdot v_2$

## Pontecorvo - 1957

## neutrino mixing

## Bruno Poniegorvo

## **1913 - 1993**



A neutrino is produced with a certain momentum. The different mass eigenstates propagate with different velocities, less than the speed of light. The composition of the neutrino state is changing.

#### neutrino oscillation



## neutrino oscillation



 $\Theta = \pi/2$ 



#### propagation of neutrino: mass eigenstate

$$\left|\nu_{i}(t)\right\rangle = e^{-i(E_{i}t - \vec{p}\vec{x})} \left|\nu_{i}(0)\right\rangle$$

$$\left| \vec{p} \right| >> m_i$$

===> 
$$E_i = \sqrt{\vec{p}^2 + m_i^2} \approx E + \frac{m_i^2}{2E}$$

$$\left|\nu_{i}(L)\right\rangle = e^{-im_{i}^{2}L/2E}\left|\nu_{i}(0)\right\rangle$$

 $f_{x} = c = 1$  $|V_{i}(t) > = e^{-i(E_{i}t - \vec{p} \cdot \vec{x})} |V_{i}(0)$  $|\vec{p_i}| \gg m_i$  $E_{i} = \overline{lp_{i}^{2}} + m_{i}^{2}$   $\cong |\vec{p}_{i}| + \frac{m_{i}^{2}}{2p_{i}} \approx E + \frac{m_{i}^{2}}{2E}$  $t \approx L$  $|v_{i}(L)\rangle = e^{-im_{i}^{2}L/2E} |v_{i}(0)\rangle$ 

 $|v_{\alpha}\rangle = \sum_{i} U_{\alpha i}^{*} / v_{i} \rangle$  $|v_i\rangle = \sum_{\alpha} U_{\alpha i} |v_{\alpha}\rangle$ 

 $V_{\alpha}: V_{e}, V_{\mu}, V_{\tau}$ Vi: 3 mass eigenstates probability to change flavor;

 $\begin{aligned} \mathcal{P}_{a \to \beta} &= \left| \langle v_{\beta} | v_{\alpha}(t) \rangle \right|^{2} \\ &= \left| \sum_{i} \mathcal{U}_{\alpha i}^{*} \mathcal{U}_{\beta i} e^{-i \cdot m_{i}^{2} L/2E} \right|^{2} \end{aligned}$ 

2 - neutrino case (v<sub>e</sub>, v<sub>m</sub>)  $\mathcal{U} \longrightarrow \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix}$  $P_{\alpha \to \beta} (\alpha \neq \beta) =$   $sin^{2} (2\theta) \cdot sin^{2} \frac{\Delta m^{2} \cdot L}{4E}$  $= \sin^{2}(2\theta) \cdot \sin^{2}(1.267 \cdot \frac{Am^{2}L}{E} + \frac{GeV}{eV^{2}km})$ 









## Kamland experiment ( Kamioka )









- Long Baseline (180 km)
- Calibrated source(s)
- Large detector (1 kton)
- Deep underground (2700 mwe)





Sudbury Neutrino Observatory



#### Sudbury Neutrino Observatory (SNO)

Schwer-Wasser-Čerenkov-Detektor
Ontario, USA

Kessel, Ø 12m 1000 t D<sub>2</sub>O

Unterstützungsstruktur 9500 PMTs (60% Abdeckung)

innere Wasserabschirmung 1700 t

äußere Wasserabschirmung 5300 t

#### Abschirmung

Sonne

Experimente I

SNP

Experimente II



# SNO

#### **charged current and neutral current**

#### neutrino oscillations:

## neutrinos



## massive fermions

## Kamiokande, SNO, Kamland neutrino mass differences

 $\Delta m_{21}^{2} \approx 8^{+0.6}_{-0.4} \cdot 10^{-5} eV^{2}$  $\Delta m^2_{32} \approx 2.4^{+0.6}_{-0.5} \cdot 10^{-3} eV^2$ 

# neutrino masses

Anne of mass term?





## Majorana massp

## Superposition of Dirac mass and Majorana mass: $M_{\nu} = \begin{bmatrix} 0 & D \\ D & M \end{bmatrix}$

 $m_{_V}$ 

#### Minkowski 1976 Yanagida Gell-Mann, Ramond, Slansky 1978

#### History of Seesaw



Footnote: H. Fritzsch, M. Gell-Mann, P. Minkowski, PLB 59 (1975) 256

This idea was very clearly elaborated by Minkowski in his paper PLB 67 (1977) 421 ---- but it was unjustly forgotten until 2004.



The idea was later on embedded into the GUT frameworks in 1979 and 1980:

- T. Yanagida 1979
- M. Gell-Mann, P. Ramond, R. Slansky 1979
- S. Glashow 1979
- R. Mohapatra, G. Senjanovic 1980

It was Yanagida who named this mechanism as "seesaw".
## **Neutrino Masses** Mass terms for charged leptons and neutrinos are not parallel -> **Neutrino Mixing** ( **Pontecorvo** ,1957... ==>)

neutrino mixing matrix (==> CKM Matrix)  $\begin{pmatrix} V_{1e} & V_{2e} & V_{3e} \end{pmatrix}$  $V_{1\mu}$  $V_{2\mu}$  $V_{3\mu}$ V = $V_{2\tau}$  $V_{1\tau}$  $V_{3\tau}$ 

 $\nu_e = V_{1e}\nu_1 + V_{2e}\nu_2 + V_{3e}\nu_3$ 

## $\nu_{\mu} = V_{1\mu}\nu_1 + V_{2\mu}\nu_2 + V_{3\mu}\nu_3$

 $\nu_{\tau} = V_{1\tau}\nu_{1} + V_{2\tau}\nu_{2} + V_{3\tau}\nu_{3}$ 







 $\theta_l \approx reactor - angle$ (unknown)

# $\frac{\text{Kamiokande, SNO}}{31.7^{\circ} \le \theta_{sun}} \le 36.3^{\circ}$

 $38^{\circ} \leq \theta_{at} \leq 52^{\circ}$ 

 $\Delta m_{21}^{2} \approx 7.6 \cdot 10^{-5} eV^{2}$  $\Delta m_{32}^{2} \approx 2.4 \cdot 10^{-3} eV^{2}$ 



$$U = \begin{bmatrix} \cos \theta_l & \sin \theta_l & 0 \\ -\sin \theta_l & \cos \theta_l & 0 \\ 0 & 0 & 1 \end{bmatrix} \bullet \begin{bmatrix} e^{-i\varphi} & 0 & 0 \\ 0 & \cos \theta & \sin \theta \\ 0 & -\sin \theta & \cos \theta \end{bmatrix} \bullet \begin{bmatrix} \cos \theta_v & -\sin \theta_v & 0 \\ \sin \theta_v & \cos \theta_v & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\tan 2\theta_l = \frac{2\sqrt{m_e m_\mu}}{m_\mu - m_e} \cong 0.0695$$

$$\tan 2\theta_{\nu} = \frac{2\sqrt{m_1 m_2}}{m_2 - m_1}$$

#### observation

## $\theta_{v} \approx 33^{\circ} = \theta \approx 45^{\circ}$

## $=>m_1/m_2 \approx 0.42_{-0.04}^{+0.12}$

## weak mass hierarchy

$$m_1 / m_2 \approx 0.42$$

 $\Delta m_{21}^{2} \approx 7.6 \cdot 10^{-5} eV^{2}$ 

 $\Delta m^2{}_{32} \approx 2.4 \cdot 10^{-3} eV^2$ 

### ==> neutrino masses



## m(1) = (0.0040 + /-0.001) eV

m(2) = (0.0096 + /- 0.002) eV

#### m(3) = (0.049 eV + /- 0.007) eV

#### normal mass hierarchy (no inversion)

#### **masses** (relative)





 $V_3$ 

## weak mass hierarchy for neutrinos $\Rightarrow$ large mixing angles

#### **Neutrino Mixing Matrix:**



#### relations between quark masses P

#### Observed:

#### m(c) : m(t) = m(u):m(c)1/207 1/207

m(s):m(b) = m(d):m(s)1/23 1/23



 $m_{o} \cong 0.511$ MeV  $m_{\mu} \cong 105.66$ MeV  $m_{\tau} \cong 1776.8$ MeV  $\frac{m_{\mu}}{\simeq} \simeq 0.0595$  $\mathcal{M}_{ au}$  $\frac{m_e}{\simeq} \simeq 0.0048$ M



#### radiative corrections

$$m(e) = m(e^{0}) + const.\left(\frac{\alpha}{\pi}\right)m(\tau) + \dots$$

 $\frac{\alpha}{\pi}m(\tau) \cong 3.95 \, MeV$ 





#### radiative corrections

$$m(e) = m(e^{0}) + const.\left(\frac{\alpha}{\pi}\right)m(\tau) + \dots$$

 $\approx 6.3 \quad MeV - 5.8 \quad MeV \approx 0.511 \quad MeV$  $m(e^0) \approx 6.3 \quad MeV$ 

#### muon and tauon not much changed by radiative corrections

$$m(\mu) = m(\mu^{o}) + const. \left(\frac{\alpha}{\pi}\right) m(\tau) + \dots$$
  

$$\approx 111.5 \quad MeV - 5.8 \quad MeV \approx 105.7 \quad MeV$$

()m<sub>µ</sub>  $\simeq 0.06$  $m_{ au}^0$ m 0.06 e $\simeq$  $\mathbf{0}$  $\widetilde{m_{\mu}}$ 



 $V_{e3} = \sin \theta_l \sin \theta_{at}$ 

 $\tan \theta_l = \sqrt{\frac{m_e^0}{m_\mu^0}} \cong 0.25$ 

## $38^{\circ} \leq \theta_{at} \leq 52^{\circ}$



# $\sin^2 2\theta_{13} \cong 0.1124 \pm 0.027$ $= 0.085 \Leftrightarrow 0.139$





#### **Double Chooz**



#### **Combined?** Best fit: $\sin^2 2\theta_{13} = 0.08$



#### Reno experiment (South Korea)



# $\sin^2 2\theta_{13} = 0.1124 \pm 0.027$ $\theta_{13} = 9.8^0 \pm 1.3^0$



#### $\sin^2 2\theta_{13} = 0.113 \pm 0.013 \pm 0.005$

## Daya Bay Experiment




### 4 reactors

#### far detector

OF

....

Bav

#### near detector

IngAo cores

100

**Daya Bay** 



# $\sin^2 2\theta_{13} = 0.1124 \pm 0.027$ $\theta_{13} = 9.8^{\circ} \pm 1.3^{\circ}$ Daya Bay

 $\sin^2 2\theta_{13} = 0.089 \pm 0.010 \pm 0.005$ 





### Majorana massp

# Majorana masses:

no fermion number neutrino = antineutrino





#### double beta decay first observed in 1987 (82 Se)

Now seen in decay of 82 Se 48 Ca 76 Ge 96 Zr Mo 116 Cd 100128 Te 130 Te 130 Ba 238 136 Xe 150 Nd

Neutrino less double - decay A e<sup>-</sup> (decay via Majorana mass term )





## **Cuoricino Experiment** Te(130)Gran Sasso Laboratory present limit Majorana eutrino mass 0.23 e

# Gran Sasso

# New experiments



Phase I:15 kg y:0.3 - 0.9 eVPhase II:37.5 kg y:0.09 - 0.29 eVPhase III:1 ton0.01 eV



Cryogenic Underground

Observatory for Rare Events

<sup>130</sup>Te

Xe- Observatory



$$m_{eff.} = V_{1e}^2 \cdot m_1 + V_{2e}^2 \cdot m_2 + V_{3e}^2 \cdot m_3 \le 0.23 \quad eV$$

#### BXDBEEBE:

#### $m_{eff.} = 0.0027 + 0.0043 + 0.0085 \approx 0.016$

$$\dots \dots V_1 \dots \dots V_2 \dots \dots V_3 \dots$$

# factor 15 improvement !?

$$U = \begin{bmatrix} \cos \theta_l & \sin \theta_l & 0 \\ -\sin \theta_l & \cos \theta_l & 0 \\ 0 & 0 & 1 \end{bmatrix} \bullet \begin{bmatrix} e^{-i\varphi} & 0 & 0 \\ 0 & \cos \theta & \sin \theta \\ 0 & -\sin \theta & \cos \theta \end{bmatrix} \bullet \begin{bmatrix} \cos \theta_\nu & -\sin \theta_\nu & 0 \\ \sin \theta_\nu & \cos \theta_\nu & 0 \\ 0 & 0 & 1 \end{bmatrix}$$



### maximal CP – violation also for neutrinos





## fermion masses remain a mystery flavor mixing angles for quarks are given by the quark mass ratios ( theory <=> experiment )

### mass matrices of quarks and leptons:

## Structure:

() A R C  $R^*$ 



# flavor mixing angles



# mass ratios of quarks / leptons

# neutrino Masses

m(1): 0.0041 eV m(2): 0.0097 eV m(3): 0.0510 eV

neutrinoless double beta decay improvement: factor 15 necessary

 $V_{e3} \approx 0.17$ 



### texture zero mass matrices

#### masses of quarks - leptons

# flavor mixing angles